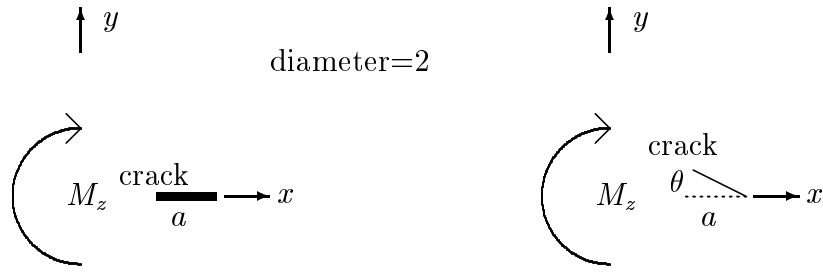


程式26 Adaptive BEM for crack



symmetry case

unsymmetry case

1. Problem statement:

$$G.E.: \quad \nabla^2 \Psi(x, y) = -2, \quad (x, y) \in D$$

$$BC: \quad \Psi(x, y) = 0, \quad (x, y) \text{ on the boundary}$$

2. By changing of variables, the problem becomes

$$G.E.: \quad \nabla^2 \Psi^*(x, y) = 0, \quad (x, y) \in D$$

$$BC: \quad \Psi^*(x, y) = (x^2 + y^2)/2, \quad (x, y) \text{ on the boundary}$$

$$\text{where } \Psi = \Psi^* - (x^2 + y^2)/2$$

3. Solve Ψ^* and the stress function Ψ by dual BEM.

4. Determine the torsion by

$$M_z = \iint_A (x\tau_{yz} - y\tau_{zx}) dx dy$$

$$\text{where } \tau_{yz} = -\alpha G \frac{\partial \Psi}{\partial x}, \tau_{zx} = \alpha G \frac{\partial \Psi}{\partial y}$$

G: shear modulus, α : the twist angle per unit length.

5. Compare the results with the following analytical solution Ψ and T :

$$\Psi(r, \phi) = 32 \frac{a^2}{\pi} \sum_{n=0}^{\infty} \frac{\left(\frac{r}{a}\right)^{(2n+1)/2} - \left(\frac{r}{a}\right)^2}{(2n+1)[16 - (2n+1)^2]} \sin \frac{(2n+1)\phi}{2}, \quad T = 0.878Ga^4\theta$$

The torsional rigidity C ($= G\pi a^4/2$ for circle) is

$$C = Ga^4 \left\{ \frac{512}{\pi} \sum_{n=0}^{\infty} \frac{1}{(2n+1)^2(2n+5)[16 - (2n+1)^2]} - \frac{\pi}{2} \right\} = 0.878Ga^4$$

6. Use equilibrium condition as an error estimator for adaptive mesh generation by

$$U_L^{-1}T_M \text{ or } L_U^{-1}M_T$$

7. Show the results of uniform and adaptive BEM meshes, stress distribution and deformed shape.

References

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