Complex Variable 作業 12 Jan.10, 2007

Given a casual function $f(t) = e^{-\xi t} \cos(t), t > 0, \text{ otherwise } f(t) = 0$

- (1) Please find $f_e(t)$ and $f_o(t)$.
- (2) Plot $f_e(t)$ and $f_o(t)$.
- (2) Please find its Fourier transform.
- (3) Check its Hilbert transform pair using complex integrals.
- (4) By taking the limit of $\xi \to 0$, recheck the results of the previous homeworks.

Hint:
$$\lim S_k(x) = \lim_{k \to 0} \frac{1}{\pi} \frac{k}{(1+k^2x^2)} = \delta(x)$$