## Complex Variable 作業 12 Jan.10, 2007

Given a casual function $\quad f(t)=e^{-\xi t} \cos (t), t>0$, otherwise $f(t)=0$
(1) Please find $f_{e}(t)$ and $f_{o}(t)$.
(2) Plot $f_{e}(t)$ and $f_{o}(t)$.
(2) Please find its Fourier transform.
(3) Check its Hilbert transform pair using complex integrals.
(4) By taking the limit of $\xi \rightarrow 0$, recheck the results of the previous homeworks.

Hint: $\lim S_{k}(x)=\lim _{k \rightarrow 0} \frac{1}{\pi} \frac{k}{\left(1+k^{2} x^{2}\right)}=\delta(x)$

