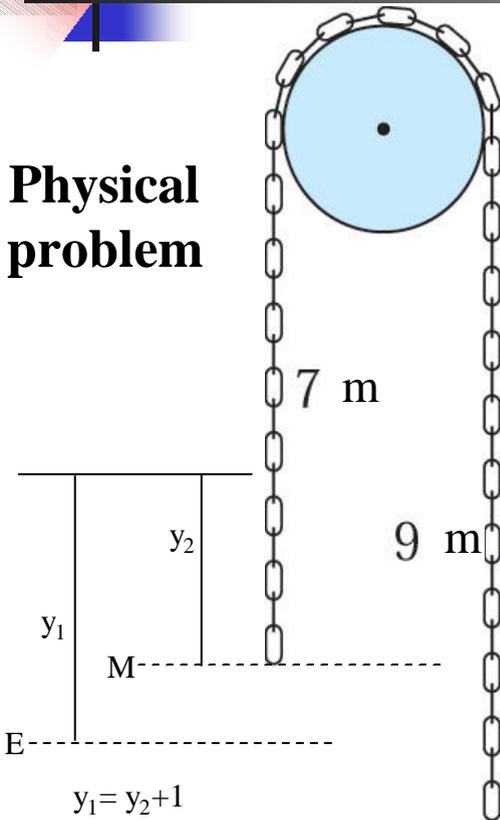


Mathematical modeling

Physical problem



	y_1 system	y_2 system
	Equilibrium (E)	Max point (M)
2nd order ODE	$16\ddot{y}_1 = 2 \times 9.8 \times y_1$ $y_1(0) = 1$ $y_1'(0) = 0$ (exam)	$16\ddot{y}_2 = 2 \times 9.8 \times (y_2 + 1)$ $y_2(0) = 0$ $y_2'(0) = 0$ (HW)
1st order ODE	$v_1 \frac{dv_1}{dy_1} = 1.23y_1$ $\frac{dy_1}{dt} = 1.11\sqrt{y_1^2 - 1}$ (exam)	$v_2 \frac{dv_2}{dy_2} = 1.23(y_2 + 1)$ $\frac{dy_1}{dt} = 1.11\sqrt{y_1^2 + 2y}$ (HW)
Comments	2nd order ODE (homogeneous ODE) (non-homogeneous BC)	2nd order ODE (non-homogeneous ODE) (homogeneous BC)
	$\int \frac{1}{\sqrt{y^2 - 1}} dy = \cosh^{-1}(y)$	$v_{es} = 8.80 \text{ m/sec}$ $t_{es} = 2.5 \text{ sec}$

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