1．Derive the closed－form solutions for the Green function and particular solution for

$$
\frac{d^{2} y(x)}{d x^{2}}+\frac{1}{4} y(x)=\sin (2 x)
$$

subject to

$$
y(0)=y(\pi)
$$

Compare the results with the series solutions in the textbook and plot．

