## 海洋大學河海工程學系九十四學年度 第一學期 □<sub>小考</sub> 考試命題紙

考試科目	開課系級	考試日期	印製份數	答案紙	命題教師	備	註
工程數學一	<u></u>	10月24日	111	■ 需	陳桂鴻 呂學育	第一次	欠大考

- **1. A Bernoulli equation of**  $xy' + y = \frac{1}{y}$ ,
  - (a) Linear or nonlinear (2%), why? (2%)
  - (b) Exact (Yes or No) (2%), why? (2%)
  - (c) Solve by Separable variable method. (6%)
  - (d) Solve by Linear O.D.E method (Convert the O.D.E to a linear equation by using the change of variable method). (7%)
  - (e) Solve by the Exact O.D.E method. (9%)
- **2.The Ricatti equation**  $y' = y^2 \frac{1}{x}y \frac{4}{x^2}$  by using the solution  $y_2 = y_1 + \frac{1}{z}$  with  $y_1 = 2/x$ , we

**obtain** 
$$y_2 = \frac{2}{x} + \frac{1}{-\frac{1}{4}x + Cx^{-3}}$$
,  $C \in \Re$ . By setting  $C = 0$ , we have  $y_2 = -\frac{2}{x}$ , solve  $y_3 = -\frac{2}{x} + \frac{1}{z}$ , please

find  $y_3$ . (10%)

3. Solve the singular solution and general solution of the Clairauts equation  $y = x \frac{dy}{dx} + f(\frac{dy}{dx})$ , where

$$f(\frac{dy}{dx}) = -e^{2y'}$$
. (10%)

- **4.** (a) is the differential equation  $(1-x)y'-4x\sin(y)=\cos(x)$  linear or nonlinear in y ? (3%)
  - (b) is the differential equation  $(y^2 1)dx = xdy$  linear or nonlinear in x? (3%)
  - (c) solve the separable differential equation  $\frac{dy}{dx} + \frac{y}{x} = 0$ , y(1) = 1 (5%)
  - (d) What is the slope of the tangent line to the graph of the solution  $y' = 6\sqrt{y} + 5x^3$  that through (-1, 1)? (4%)
  - (e) Match the given differential equations with one or more of the solutions

(a) 
$$y = 0$$
, (b)  $y = 2$ , (c)  $y = 2 + 2x^2$ , (d)  $y = 2x^2$ , (e)  $y = -2x^2$  (5%)  $x \frac{dy}{dx} = 2y$ ;  $\frac{dy}{dx} = 2y - 4$ 

**5. Solve the initial-value problem**  $\frac{dy}{dx} = (3x - y)^2 + 6x - 2y$ , y(0) = -3 (15%)

$$6.(2y\sin x - 3)dx - \cos xdy = 0$$

- (a) Is it exact? (2%) Why? (3%)
- (b) Solve it by using an integrating factor. (10%)