

1, Find the general solution using the method of variation of parameters

$$y'' + 9y = 12 \sec(3x)$$

2, Find the general solution using the method of undetermined coefficients

$$y'' + 4y' + 4y = 7x - 3 \cos(2x) + 5x e^{-2x}$$

3, Show that $y_1(x) = x^2$ and $y_2(x) = x - 1$ are solutions of $(x^2 - 2x)y'' + 2(1-x)y' + 2y = 0$, use this to find the general solution of $(x^2 - 2x)y'' + 2(1-x)y' + 2y = 6(x^2 - 2x)^2$

4, Find the general solution of the differential equation or the solution of the initial value problem

$$yy'' - 2(y')^2 = 0$$