

- 1, Find the eigenvalues of the matrix and for each eigenvalue, a corresponding eigenvector.

Check that eigenvectors associated with distinct eigenvalues are orthogonal.

Find an orthogonal matrix that diagonalizes the matrix. (P362, Problem 11)

$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 0 & 1 & -2 & 0 \\ 0 & -2 & 1 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}$$

- 2, Find the standard form of the quadratic form.

$$-2x_1x_2 + 2x_3^2$$

- 3, Use the principal axis theorem to analyze the conic

$$3x_1^2 + 5x_1x_2 - 3x_2^2 = 5$$

- 4, Revisit Example Problem 8.17 and calculate the angle of the  $y_1$  axis relative to the  $x_1$  axis, as shown in Figure 8.2