

HW.2 (Integrating Factor, Homogeneous, Bernoulli, Riccati Equations)

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1. Consider  $y - xy' = 0$ .
  - a. Show that this equation is not exact on any rectangle.
  - b. Find an integrating factor  $\mu(x)$  that is a function of  $x$  alone.
  - c. Find an integrating factor  $\nu(y)$  that is a function of  $y$  alone.
  - d. Show that there is also an integrating factor  $\eta(x,y) = x^a y^b$  for some constant  $a$  and  $b$ . Find all such integrating factor.  
(Page 39, Problem 3.)
  
2. Find the general solution. These problems include all types considered in this section.
  - a.  $y' + xy = xy^2$  (Page 46, Problem 3.)
  - b.  $(x - 2y)y' = 2x - y$  (Page 46, Problem 7.)
  - c.  $y' = -e^{-x}y^2 + y + e^x$  (Page 46, Problem 13.)