

國立台灣海洋大學 2005 河工系工程數學(二) 第二次作業題目

13.5

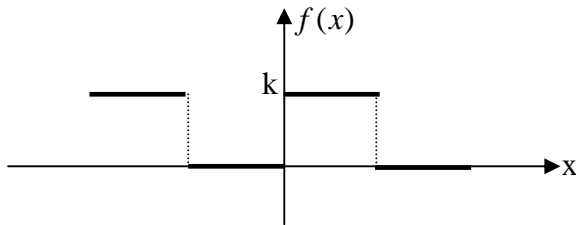
2. Let $f(x) = |x|$ for $-1 \leq x \leq 1$.

- (a) Write the Fourier series for $f(x)$ on $[-1,1]$.
- (b) Show that this series can be differentiated term-by-term to yield the Fourier expansion of $f'(x)$ on $[-1,1]$.
- (c) Determine $f'(x)$ and write its Fourier series on $[-1,1]$. Compare this series with that obtained in (b).

13.6

Find the phase angle form of the Fourier series of the function.

12.



15. The RMS (root mean square) value of a function f over an interval $[a,b]$ is

defined to be
$$RMS(f) = \sqrt{\frac{\int_a^b [f(x)]^2 dx}{b-a}}$$
. If f is periodic, this quantity is

evaluated over an interval of length equal to the fundamental period of f .

Determine $RMS(E \sin(\omega x))$, with E and ω positive constants.

13.7

Write the complex Fourier series of f , Determine what this series converges to, and plot some points of the frequency spectrum. Keep in mind that in specifying a function of period p , it is sufficient to define $f(p)$ on any interval of length p .

5. f has period 4 and
$$f(x) = \begin{cases} -1 & \text{for } 0 \leq x < 2 \\ 2 & \text{for } 2 \leq x < 4 \end{cases}$$

12. Plot the phase spectrum of the periodic function of Problem 5.