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海洋大學河海工程學系2004 工程數學(三)第二次小考參考解答

1. Given a spiral curve, we can describe by time-like parameter as follows:

$$x(t) = 4\cos(t), y(t) = 4\sin(t), z(t) = 3t \mathbf{r}(t) = (x(t), y(t), z(t))$$

Please describe the curve by using space-like parameter (arc length s).

Ans: $\mathbf{r}(s) = (\cos(s/5), \sin(s/5), s/5).$

2. Plot the curve from the starting point of (4,0,0)?

3. What is the distance of the arc length of the curve from t = 0 to $t = 2\pi$? Ans: 10π .

4. Please determine the radius of curvature for ρ and σ as shown below:

Ans: $\rho = 25/4, \sigma = 25/3$

5. Determine

$$\left(\frac{d\mathbf{r}}{ds} \times \frac{d^2\mathbf{r}}{ds^2}\right) \cdot \frac{d^3\mathbf{r}}{ds^3}$$

Ans: $\frac{1}{\rho^2 \sigma} = 48/125^2$